## Sudden Contraction Rounded Circular Cross-Section <br> (Pipe Flow - Guide)



## Model description:

This model of component calculates the minor head loss (pressure drop) generated by the flow in a sudden contraction rounded.

The head loss by friction in the inlet and outlet piping is not taken into account in this component.

## Model formulation:

Ratio of small to large diameter:

$$
\beta=\frac{d_{2}}{d_{1}}
$$

Major cross-sectional area $\left(m^{2}\right)$ :
$A_{1}=\pi \cdot \frac{d_{1}^{2}}{4}$

Minor cross-sectional area ( $m^{2}$ ):
$\mathrm{A}_{2}=\pi \cdot \frac{d_{2}{ }^{2}}{4}$

Mean velocity in major diameter ( $\mathrm{m} / \mathrm{s}$ ):
$V_{1}=\frac{Q}{A_{1}}$

Mean velocity in minor diameter $(\mathrm{m} / \mathrm{s})$ :

$$
V_{2}=\frac{Q}{A_{2}}
$$

Mass flow rate ( $\mathrm{kg} / \mathrm{s}$ ):

$$
G=Q \cdot \rho
$$

Reynolds number in major diameter:
$N_{\text {Re }_{1}}=\frac{V_{1} \cdot d_{1}}{v}$

Reynolds number in minor diameter:

$$
N_{\mathrm{Re}_{2}}=\frac{V_{2} \cdot d_{2}}{v}
$$

Jet contraction coefficient:
■ $0 \leq r / d_{2} \leq 1$ :

$$
\lambda=1+0.622 \cdot\left(1-0.30 \cdot \sqrt{\frac{r}{d_{2}}}-0.70 \cdot \frac{r}{d_{2}}\right)^{4} \cdot\left(1-0.215 \cdot \beta^{2}-0.785 \cdot \beta^{5}\right)
$$

([1] equation
10.7)


- $r / d_{2}>1$ :
$\lambda=1$

Local resistance coefficient ( $\mathrm{NRe}_{2} \geq 10^{4}$ ):

- $0 \leq r / d_{2} \leq 1$ :

$$
K_{2}=0.0696 \cdot\left(1-0.569 \cdot \frac{r}{d_{2}}\right) \cdot\left(1-\sqrt{\frac{r}{d_{2}}} \cdot \beta\right) \cdot\left(1-\beta^{5}\right) \cdot \lambda^{2}+(\lambda-1)^{2}
$$



- $r / d_{2}>1$ :
$K_{2}=0.030 \cdot(1-\beta) \cdot\left(1-\beta^{4}\right)$
([1] equation 10.8)


Total pressure loss coefficient (based on mean velocity in minor diameter):
$K=K_{2}$

Total pressure loss $(\mathrm{Pa})$ :
$\Delta P=K \cdot \frac{\rho_{m} \cdot v_{2}^{2}}{2}$
$\Delta H=K \cdot \frac{v_{2}{ }^{2}}{2 \cdot g}$

Hydraulic power loss (W):
$W h=\Delta P \cdot Q$

## Symbols, Definitions, SI Units:

$d_{1} \quad$ Major diameter ( $m$ )
$\mathrm{d}_{2} \quad$ Minor diameter (m)
$\beta \quad$ Ratio of small to large diameter ()
$A_{1} \quad$ Major cross-sectional area ( $\mathrm{m}^{2}$ )
$A_{2} \quad$ Minor cross-sectional area ( $\mathrm{m}^{2}$ )
$Q \quad$ Volume flow rate ( $\mathrm{m}^{3} / \mathrm{s}$ )
$G \quad$ Mass flow rate ( $\mathrm{kg} / \mathrm{s}$ )
$V_{1} \quad$ Mean velocity in major diameter ( $\mathrm{m} / \mathrm{s}$ )
$V_{2} \quad$ Mean velocity in minor diameter ( $\mathrm{m} / \mathrm{s}$ )
NRe $_{1} \quad$ Reynolds number in major diameter ()
$\mathrm{NRe}_{2}$ Reynolds number in minor diameter ()
$r \quad$ Radius of the round ( $m$ )
$\lambda \quad$ Jet contraction coefficient ()
$\mathrm{K}_{2} \quad$ Local resistance coefficient ()
K Total pressure loss coefficient (based on mean velocity in minor diameter) ()
$\Delta \mathrm{P} \quad$ Total pressure loss ( Pa )
$\Delta H \quad$ Total head loss of fluid (m)
Wh Hydraulic power loss (W)
$\rho_{m} \quad$ Fluid density $\left(\mathrm{kg} / \mathrm{m}^{3}\right)$
$v \quad$ Fluid kinematic viscosity ( $\mathrm{m}^{2} / \mathrm{s}$ )
$9 \quad$ Gravitational acceleration $\left(\mathrm{m} / \mathrm{s}^{2}\right)$

## Validity range:

- turbulent flow regime in minor diameter ( $\mathrm{NRe}_{2} \geq 10^{4}$ )
- round radius less than the radius difference ( $r<\left(d_{1} / 2-d_{2} / 2\right)$ )


## Example of application:



Fluid characteristics
Fluid: Water @ $1 \mathrm{~atm}[\mathrm{HC}]$ Ref.: IAPWS IF97


| Density : | $\rho$ | 998.2061 | $\mathrm{~kg} / \mathrm{m}^{3}$ |
| :--- | :---: | ---: | :--- |
| Dynamic Viscosity: | $\mu$ | 0.00100159 | $\mathrm{~N} . \mathrm{s} / \mathrm{m}^{2}$ |
| Kinematic Viscosity: | v | $1.00340 \mathrm{E}-06$ | $\mathrm{~m}^{2} / \mathrm{s}$ |



## Divers

## Geometrical characteristics

Help Info
Calculate


Complementary results

| Designation | Symbol | Value | Unit |
| :---: | :---: | :---: | :---: |
| Diameters ratio (d2/d1) | $\beta$ | 0.6130868 |  |
| Major cross-section area | A1 | 0.003881508 | $\mathrm{m}^{2}$ |
| Minor cross-section area | A2 | 0.001458963 | $\mathrm{m}^{2}$ |
| Cross-sections area ratio | A2/A1 | 0.3758754 |  |
| Ratio 'Radius of the round / small diameter' | r/d2 | 0.1160093 |  |
| Major diameter Reynolds number | NRe1 | 90251 |  |
| Minor diameter Reynolds number | NRe2 | 147207.5 |  |
| Jet velocity ratio (Equation 10.7) | $\lambda$ | 1.235441 |  |
| Coefficient of local resistance (Equation 10.6) | K2 | 0.1271336 |  |
| Pressure loss coefficient (based on velocity in minor diameter) | K | 0.1271336 |  |
| Hydraulic power loss | Wh | 3.726247 | w |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

## References:

[1] Pipe Flow: A Practical and Comprehensive Guide. Donald C. Rennels and Hobart M. Hudson. (2012)

## HydrauCalc

Edition: January 2020
© François Corre 2020

